

# Mark Scheme (Results) January 2010

**GCE** 

Decision Mathematics D1 (6689)



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### January 2010 6689 Decision Mathematics D1 Mark Scheme

Question Number			Scheme		N	⁄larks
Q1(a) Q1(b)		A • B • A • B •	1 2 3 4 5 6	Initial map	B1	(1)
		C D E	2 3 4 5 6	B 2 3 3 D 4 4 5 5 6		
	E.g.		Path 1 Path 2 Matching	F-4-D-5-E-2 B-3-C-6 A: 1, B: 3, C: 6, D: 5, E: 2, F: 4	M1 M1 A1	
						[6]

Question Number	Scheme												
Q1(b)	Question 1(b) Alternative Solutions												
		Path 1	Path 2	Path 2   Matching   A   B   C   D   E   F									
	1	B-3-C-1-A-2	F-3-B-4-D-5-E-1-C-6	2	4	6	5	1	3				
	2	B-3-C-1-A-2	F-3-B-4-D-5-E-2-A-1-C-6	1	4	6	5	2	3				
	3	B-3-C-1-A-2	F-4-D-5-E-1-C-6	2	3	6	5	1	4				
	4	B-3-C-1-A-2	F-4-D-5-E-2-A-1-C-6	1	3	6	5	2	4				
	5	B-3-C-4-D-5-E-1-A-2	F-3-B-4-C-6	2	4	6	5	1	3				
	6	B-3-C-4-D-5-E-1-A-2	F-4-C-6	2	3	6	5	1	4				
	7	B-3-C-6	F-3-B-4-D-5-E-1-A-2	2	4	6	5	1	3				
	8	B-3-C-6	F-3-B-4-D-5-E-2	1	4	6	5	2	3				
	9	B-3-C-6	F-4-D-5-E-1-A-2	2	3	6	5	1	4				
	10	B-3-C-6	F-4-D-5-E-2	1	3	6	5	2	4				
	11	B-4-D-5-E-2	F-3-C-6	1	4	6	5	2	3				
	12	B-4-D-5-E-2	F-4-B-3-C-6	1	3	6	5	2	4				
	13	B-4-D-5-E-1-A-2	F-3-C-6	2	4	6	5	1	3				
	14	B-4-D-5-E-1-A-2	F-4-B-3-C-6	2	3	6	5	1	4				
	15	F-3-C-1-A-2	B-3-F-4-D-5-E-1-C-6	2	3	6	5	1	4				
	16	F-3-C-1-A-2	B-3-F-4-D-5-E-2-A-1-C-6	1	3	6	5	2	4				
	17	F-3-C-1-A-2	B-4-D-5-E-1-C-6	2	4	6	5	1	3				
	18	F-3-C-1-A-2	B-4-D-5-E-2-A-1-C-6	1	4	6	5	2	3				
	19	F-3-C-4-D-5-E-1-A-2	B-3-F-4-C-6	2	3	6	5	1	4				
	20	F-3-C-4-D-5-E-1-A-2	B-4-C-6	2	4	6	5	1	3				
	21	F-3-C-6	B-3-F-4-D-5-E-1-A-2	2	3	6	5	1	4				
	22	F-3-C-6	B-3-F-4-D-5-E-2	1	3	6	5	2	4				
	23	F-3-C-6	B-4-D-5-E-1-A-2	2	4	6	5	1	3				
	24	F-3-C-6	B-4-D-5-E-2	1	4	6	5	2	3				
	25	F-4-D-5-E-2	B-3-C-6	1	3	6	5	2	4				
	26	F-4-D-5-E-2	B-4-F-3-C-6	1	4	6	5	2	3				
	27	F-4-D-5-E-1-A-2	B-3-C-6	2	3	6	5	1	4				
	28	F-4-D-5-E-1-A-2	B-4-F-3-C-6	2	4	6	5	1	3				
	Notes  (a) B <sup>-</sup> (b) M A1 Mi	1 cao preferably just 4 ling 1 attempt at a path from E 1 correct path—including o 1 attempt at a second path 1 correct path—including o	es, but accept if unambiguous. 3 or F to 2 or 6 change status					twi					

Question Number	Scheme	Marks	
Q2(a)	<ul> <li>(i) All pairs of vertices connected by a path, but not describing complete graph.</li> <li>(ii) No cycles</li> <li>(iii) All nodes connected (accept definition of minimum spanning tree)</li> </ul>	B1 B1 B1	(3)
Q2(b)	Kruskal's (algorithm)	B1	(1)
Q2(c)(i)	L-O 56 L-C 60 C-N 62 O-S 63 S-P 43 C-Y 156 Total length 440 (miles)  Using Prim. first 2 correct  Next 2  Finish  Total	M1 A1 A1 A1 A1 =B1	
Q2(c)(ii)	Tree correct	B1	(5)
			[9]

Q2(c)

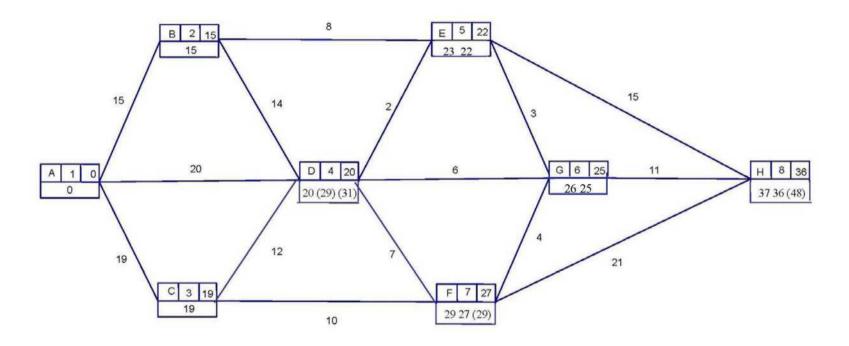
Accept weights as indicating arcs.

Misreads – award M1 A0 A0 for these:

- Vertices, not edges given LOCNSPY
- Numbers across top, edges either incorrect or not given: 3 1 4 2 6 5 7.

Also accept these, misreading And not starting at L-again M1A0A0

Started at	Minimum arcs	nodes	Numbers
С	CL,LO,CN,	CLONSPY	1243657
N	NC,CL,LO,OS,SP,CY	NCLOSPY	2314657
0	OL,LC,CN,OS,	OLCNSPY	3241657
Р	PS,SO,OL,LC,CN.CY	PSOLCNY	5463127
S	SP.SO,	SPOLCNY	5463217
Υ	YC,CL,LO,CN,	YCLONSP	2354761



Clear method to include at least	l update
(look at E, F, G or H)	M1
BCDE correct	A1
FGH correct	A1ft
Route ADEGH	A1
Total time 36 Minutes	A1ft (5)

Question Number	Scheme	Marks
Q3(b)	Odd nodes are A, B, C, H	M1
	AB + CH = 15 + 25 = 40	A1
	AC + BH = 19 + 22 = 41	A1
	AH + BC = 36 + 22 = 58	A1
	(40 is the shortest, repeating AB and CF + FG + GH)	
	Must be choosing from at least two pairings for this last mark  Shortest time = $167 + 40 = 207$ minutes. $167 + \text{their shortest}$	A1ft (5)
		[10]

Question Number					Sc	heme						M	arks
Q4(a)	0.6	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	2.6		
	4.0	3.2	4.0	2.6	0.6	2.5	0.5	0.4	0.3	1.0	3.2 0.4	M1	
	4.0	4.0	<u>3.2</u>	<u>2.6</u>	0.6	2.5	0.5	1.0	<u>0.4</u>	0.3	4.0 0.5	A1	
	4.0	4.0	<u>3.2</u>	<u>2.6</u>	0.6	2.5	1.0	<u>0.5</u>	<u>0.4</u>	0.3	2.5	A1ft	
	<u>4.0</u>	4.0	3.2 3.2 3.2	<u>2.6</u>	<u>2.5</u>	0.6	1.0	$\frac{0.5}{0.5}$	0.4	<u>0.3</u>	1.0	A1ft	
	<u>4.0</u>	<u>4.0</u>	<u>3.2</u>	<u>2.6</u>	2.5	<u>1.0</u>	0.6	<u>0.5</u>	<u>0.4</u>	$\frac{0.3}{0.3}$		A1 c	SO
													(5)
Q4(b)			ength 1:										
			ength 3:		0.6			left col	ıımn & 1	1.0 in plac	e	M1	
			ength 4:		1.0	0.4		1011 001		0.6 & 0.5	~	A1	
			ength 5:		0.5	0.3				0.4		A1	
			C							All correc	t (c.s.o)	A1	
													(4)
Q4(c)	19.1/4	4 = 4.77								0.9 'spar	e .	B1	
			Yes, t	he answ	er to (t	o) does u	se the n	ninimur	n numbe	er of bins.		DB1	
													(2)
ı													[11]

#### Notes for Q4(a)

1M1 Pivot, p, chosen. List sorted, >p, p. p. If only choosing 1 pivot per iteration M1 only

1A1 1<sup>st</sup> pass correct and chosen next **two** pivots correctly for sublists >1

2A1ft 2<sup>nd</sup> pass correct and chosen next **two** pivots correctly for sublists >1

3A1ft 3<sup>rd</sup> pass correct and next pivot for sublist >1 chosen correctly.

4A1 cso.

#### Misread in part (a)

- If they have misread a number at the start of part (a), so genuinely miscopied and got for example 0.1 instead of 1.0 then mark the whole question as a misread removing the last two A or B marks earned. This gives a maximum total of 9.
- If they misread their own numbers **during the course of part** (a) then count it as an **error in part** (a) but mark parts (b) and (c) as a misread. So they would lose marks in (a) for the error and then the last two A or B marks earned in (b) and (c) giving a maximum of 8 or maybe 7 marks depending on how many marks they lose in (a).

The most popular misread is the one listed above – where 1.0 has changed to 0.1 giving

4.0 4.0 3.2 2.6 2.5 0.6 0.5 0.4 0.3 **0.1** at the end of (a) for this one (b) and (c) are:

(b) Length 1: 4

Length 2: 4

Length 3: 3.2 0.6 0.1

Length 4: 2.6 0.5 0.4 0.3

Length 5: 2.5

(c) 18.2/4 = 4.55 so 5 bins, or total is 18.2 or 1.8 'spare' Yes answer in (b) uses the minimum number of bins.

#### Alternate solutions for Question 4

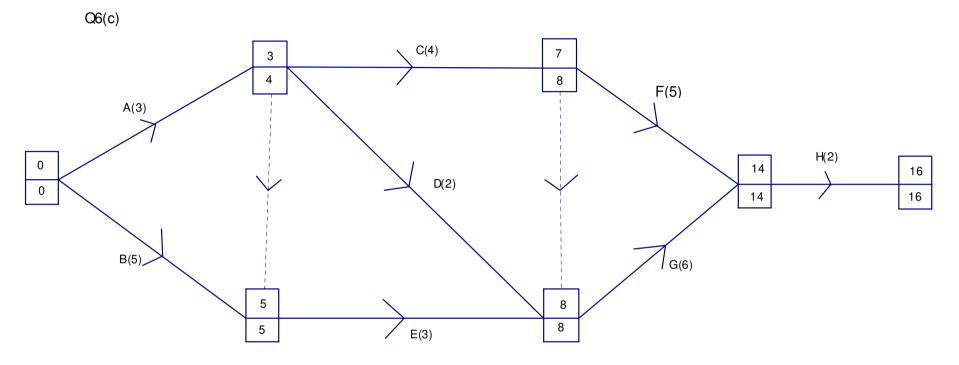
Choos 0.6 0.6 4.0 4.0 4.0	4.0 4.0 4.0 4.0 4.0 <b>4.0</b> <b>4.0</b>	ddle lef 2.5 2.5 3.2 3.2 3.2 3.2	3.2 3.2 0.6 2.6 2.6 2.6	0.5 2.6 2.5 <b>2.5</b> <b>2.5</b> <b>2.5</b>	2.6 4.0 2.6 0.6 1.0	0.4 1.0 1.0 1.0 0.6 0.6	0.3 0.5 0.5 0.5 0.5	4.0 <u>0.4</u> <b>0.4</b> <b>0.4</b> <b>0.4</b> <b>0.4</b>	1.0 0.3 <u>0.3</u> <b>0.3</b> <b>0.3</b> <b>0.3</b>	(pivot 0.5) (pivots 3.2, 0.4) (pivots 4.0, 2.5) (pivots 0.6)
Choos <u>0.6</u> <u>4.0</u> <b>4.0</b> <b>4.0</b> <b>4.0</b> <b>4.0</b> <b>4.0</b>	4.0 2.5 <u>2.5</u> <u>3.2</u> 4.0 <b>4.0</b>	2.5 3.2 3.2 2.6 3.2 3.2	3.2 2.6 2.6 4.0 <u>2.6</u> <b>2.6</b>	0.5 4.0 4.0 <b>2.5</b> <b>2.5</b> <b>2.5</b>	2.6 1.0 1.0 1.0 1.0	0.4 0.6 0.6 0.6 0.6	0.3 <u>0.5</u> <b>0.5</b> <b>0.5</b> <b>0.5</b> <b>0.5</b>	4.0 0.4 <u>0.4</u> <b>0.4</b> <b>0.4</b>	1.0 0.3 0.3 <u>0.3</u> <b>0.3</b>	(pivot 0.6) (pivots 4.0, 0.5) (pivots 2.5, 0.4) (pivots 3.2)
OR (a <u>0.6</u> <u>4.0</u> <u>4.0</u> <b>4.0</b> <b>4.0</b> <b>4.0</b> <b>4.0</b>	4.0 2.5 4.0 4.0 4.0 4.0	e choos 2.5 3.2 <u>2.5</u> 3.2 3.2 3.2	3.2 2.6 3.2 2.6 2.6 2.6	0.5 4.0 2.6 <b>2.5</b> <b>2.5</b> <b>2.5</b>	2.6 1.0 1.0 <u>1.0</u> 1.0	0.4 0.6 0.6 0.6 0.6	0.3 <u>0.5</u> <b>0.5</b> <b>0.5</b> <b>0.5</b> <b>0.5</b>	4.0 0.4 <u>0.4</u> <b>0.4</b> <b>0.4</b>	1.0 0.3 0.3 <u>0.3</u> <b>0.3</b>	(pivot 0.6) (pivots 4.0, 0.5) (pivots 2.5, 0.4) (pivots 3.2)

Question 4 sorting into ASCENDING order	full marks if then reversed.	otherwise MISREAD)

Middl	le left									
0.6	4.0	2.5	3.2	<u>0.5</u>	2.6	0.4	0.3	4.0	1.0	(pivot 0.5)
0.4	0.3	0.5	0.6	4.0	2.5	3.2	2.6	4.0	1.0	(pivot 0.4, 3.2)
0.4 0.3	0.4	0.5	0.6	<u>2.5</u>	2.6	1.0	3.2	<u>4.0</u>	4.0	(pivot 2.5, 4.0)
0.3	0.4	0.5	<u>0.6</u>	1.0	2.5	<u>2.6</u>	3.2	4.0	4.0	(pivot 0.6)
0.3	0.4	0.5	0.6	1.0	2.5	2.6	3.2	4.0	4.0	
Middl	le right									
0.6	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	(pivot 2.6)
0.6	2.5	0.5	0.4	0.3	1.0	2.6	4.0	3.2	4.0	(pivot 0.4, 3.2)
0.3	0.4	0.6	2.5	<u>0.5</u>	1.0	2.6	3.2	4.0	4.0	(pivot 0.5, 4.0)
0.3	0.4	0.5	0.6	2.5	1.0	2.6	3.2	4.0	4.0	(pivot 2.5)
0.3	0.4	0.5	0.6	1.0	2.5	2.6	3.2	4.0	4.0	(pivot 1.0)
First	/1\									
0.6	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	(pivot 0.6)
0.0	0.4	0.3	0.6		2.5	3.2	2.6	4.0	1.0	(pivot 0.5, 4.0)
0.5	0.3	0.5	0.6	4.0 2.5	3.2	2.6	1.0	4.0	4.0	(pivots 0.4, 2.5)
0.5 0.4 0.3	0.4	0.5	0.6	1.0	2.5	3.2	2.6	4.0	4.0	(pivots 3.2)
0.3	0.4	0.5	0.6	1.0	2.5	<u>3.2</u> 2.6	3.2	4.0	4.0	(p://oto/o.2)
First										
0.6	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	(pivot 0.6)
0.5 0.4 0.3	0.4	0.3	0.6	4.0	2.5	3.2	2.6	4.0	1.0	(pivot 0.5, 4.0)
0.4	0.3	0.5	0.6	2.5	3.2	2.6	1.0	4.0	4.0	(pivots 0.4, 2.5)
0.3	0.4	0.5	0.6	1.0	2.5	3.2	2.6	4.0	4.0	(pivots 3.2)
0.3	0.4	0.5	0.6	1.0	2.5	2.6	3.2	4.0	4.0	•

Question Number			5	Scheme			Ma	arks
Q5	S	Т	R	R>0?	Output			
(a)	25000	0	17000	y y	Output	Line 1		
(α)	23000	3400	17000	y		Line 2		
		3100	7000			Line 3		
			,,,,,	у		Line 4		
		4450				Line 5		
			-5000			Line 6		
				n		Line 7		
					4450			
						Lines 1 & 2: Lines 3-7:	M1A1 M1A1	
						Output correct:	A1	(5)
(h)	TD	025.000: /	04450				D1ft	
(b)	Tax on a	£25 000 is £	E4450				B1ft	(1)
(c)	Tax free	sum = £80	000:				B1	(4)
								(1)
								[7]

Question Number		Scheme										
Q6(a)	The o	The dotted line represents a dummy activity.  It is necessary because C and D depend only on A, but E depends on A and B.										
Q6(b)		Activity	Immediately preceding activity									
		A	-									
		В	-									
		С	A									
		D	A	To this point	B1							
		Е	A,B									
		F	C (A)	For E & F, accepting correct "extra"	B1							
		G	C, D, E									
		Н	F, G	Last two rows, correct only,	B1	(3)						



Early times M1A1 Late times M1A1 (4)

Q6(d) Critical activities: B, E, G, H

Critical path: 16 days

B1ft (2)

B1

Question Number	Scheme	Marks
Q6(e)	0 2 4 6 8 10 12 14 16 18 20	
	At least 6 activities placed including at least 3 floats	M1
	Critical Activities	A1
	A + C	
	D + F	A1 (4)
		[15]

Question Number	Scheme	Mark	(S
Q7(a)	$x + 2y \le 12$ $(150x + 300y \le 1800)$	M1A1	(2)
Q7(b)	$0.9x + 1.2y \le 9 \\ \to 3x + 4y \le 30  (*)$	M1 A1 cso	(2)
Q7(c)	(You need to buy) at least 2 large cupboards.	B1	(1)
Q7(d)	Capacity C and 140%C So total is $Cx + \frac{140}{100}Cy$ Simplify to $7y + 5x$ (*)	M1 A1cso	(2)
Q7(e)	y $8$ $3x + 4y = 30$ $6$ $5$ $4$ $3$ $2$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$ $7$		
	$y \ge 2$ $0.9x + 1.2y \le 12  (3x + 4y \le 30)$ $x + 2y \le 12  (150x + 300y \le 1800)$ Lines labelled & drawn with a ruler	B1 B1 B1 B1	
	Shading, Region identified	B1, B1	(6)
Q7(f)	Consider points and value of $5x + 7y$ : Or draw a clear profit line $(7,2) \rightarrow 49 \text{ or } (7 \frac{1}{3},2) \rightarrow 50 \frac{2}{3}, \text{ or } (7.3, 2) \rightarrow 50.5$	M1A1	
	$ \begin{array}{rcl} (6,3) & \rightarrow & 51 \\ (0,6) & \rightarrow & 42 \\ (0,2) & \rightarrow & 14 \end{array} $	A1	
	Best option is to buy 6 standard cupboards and 3 large cupboards.	A1	(4)
			[17]

#### Question 7 notes

- (a) 1M1 correct terms, accept = here, accept swapped coefficients.
  - 1A1 cao does not need to be simplified.
- (b) 1M1 correct terms, must deal with cm/m correctly, accept = here.
  - 1A1 cso answer given.
- (c) 1B1 cao 'at least' and '2' and 'large'.
- (d) 1M1 1.4 or  $5 \times 40\%$  maybe 5+2 seen, they **must** be **seen** to engage with 140% in some way.
  - 1A1 cso answer given.

#### Lines should be within 1 small square of correct point at axes.

- (e) 1B1 correctly drawing y = 2.
  - 2B1 correctly drawing 3x + 4y = 30 [0.9x + 1.2y = 12]
- 3B1 correctly drawing x + 2y = 12 [150x + 300y = 1800], ft only if swapped coefficients in (a) (6,0) (2,8).

## These next 3 marks are only available for candidates who have drawn at least 2 lines, including at least one 'diagonal' line with negative gradient.

- 4B1 Ruler used. At least 2 lines labelled including one 'diagonal' line.
- 5B1 Shading, or R correct, b.o.d. on their lines.
- 6B1 all lines and R correct.
- (f) 1M1 At least 2 points tested **or** objective line drawn with correct m or 1/m, minimum intercepts 3.5 and 2.5.
  - 1A1 − 2 points correctly tested **or** objective line correct.
  - 2A1 3 points correctly tested **or** objective line correct and distinct/labelled.
  - 3A1 6 standard and 3 large, accept (6,3) if very clearly selected in some way.



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