

Mark Scheme (Results) January 2010

GCE

Decision Mathematics D1 (6689)

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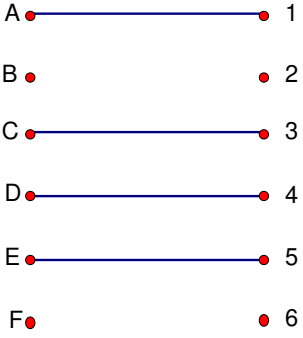
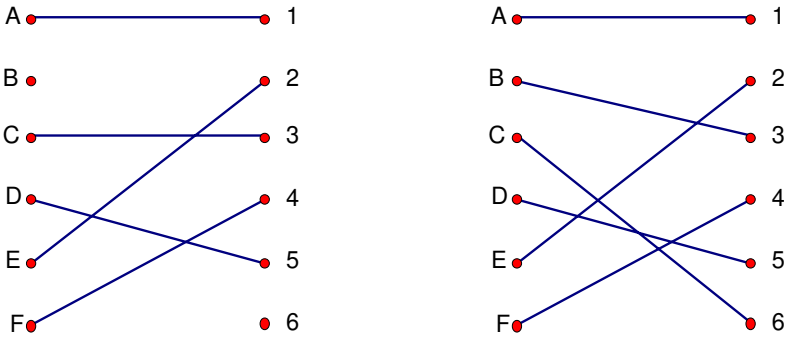
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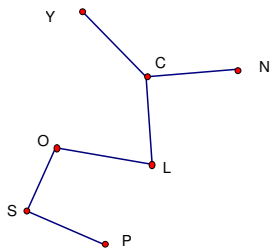
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6689 Decision Mathematics D1
Mark Scheme

Question Number	Scheme	Marks												
Q1(a)	 <p style="text-align: right; margin-right: 50px;">Initial map</p>	B1 (1)												
Q1(b)		<p>E.g.</p> <table style="width: 100%; border: none;"> <tr> <td style="width: 30%; text-align: center;">Path 1</td> <td style="text-align: center;">F-4-D-5-E-2</td> <td style="width: 20%;"></td> <td style="width: 20%; text-align: center;">M1 A1</td> </tr> <tr> <td style="text-align: center;">Path 2</td> <td style="text-align: center;">B-3-C-6</td> <td></td> <td style="text-align: center;">M1 A1</td> </tr> <tr> <td style="text-align: center;">Matching</td> <td style="text-align: center;">A : 1, B : 3, C : 6, D : 5, E : 2, F : 4</td> <td></td> <td style="text-align: center;">A1</td> </tr> </table> <p style="text-align: right; margin-right: 50px;">(5)</p> <p style="text-align: right; margin-right: 50px;">[6]</p>	Path 1	F-4-D-5-E-2		M1 A1	Path 2	B-3-C-6		M1 A1	Matching	A : 1, B : 3, C : 6, D : 5, E : 2, F : 4		A1
Path 1	F-4-D-5-E-2		M1 A1											
Path 2	B-3-C-6		M1 A1											
Matching	A : 1, B : 3, C : 6, D : 5, E : 2, F : 4		A1											

Question Number	Scheme							Marks		
Q1(b)	Question 1(b) Alternative Solutions									
		Path 1	Path 2	Matching						
				A	B	C	D		E	F
	1	B-3-C-1-A-2	F-3-B-4-D-5-E-1-C-6	2	4	6	5		1	3
	2	B-3-C-1-A-2	F-3-B-4-D-5-E-2-A-1-C-6	1	4	6	5		2	3
	3	B-3-C-1-A-2	F-4-D-5-E-1-C-6	2	3	6	5		1	4
	4	B-3-C-1-A-2	F-4-D-5-E-2-A-1-C-6	1	3	6	5		2	4
	5	B-3-C-4-D-5-E-1-A-2	F-3-B-4-C-6	2	4	6	5		1	3
	6	B-3-C-4-D-5-E-1-A-2	F-4-C-6	2	3	6	5		1	4
	7	B-3-C-6	F-3-B-4-D-5-E-1-A-2	2	4	6	5		1	3
	8	B-3-C-6	F-3-B-4-D-5-E-2	1	4	6	5		2	3
	9	B-3-C-6	F-4-D-5-E-1-A-2	2	3	6	5		1	4
	10	B-3-C-6	F-4-D-5-E-2	1	3	6	5		2	4
	11	B-4-D-5-E-2	F-3-C-6	1	4	6	5		2	3
	12	B-4-D-5-E-2	F-4-B-3-C-6	1	3	6	5		2	4
	13	B-4-D-5-E-1-A-2	F-3-C-6	2	4	6	5		1	3
	14	B-4-D-5-E-1-A-2	F-4-B-3-C-6	2	3	6	5		1	4
	15	F-3-C-1-A-2	B-3-F-4-D-5-E-1-C-6	2	3	6	5		1	4
	16	F-3-C-1-A-2	B-3-F-4-D-5-E-2-A-1-C-6	1	3	6	5		2	4
	17	F-3-C-1-A-2	B-4-D-5-E-1-C-6	2	4	6	5		1	3
	18	F-3-C-1-A-2	B-4-D-5-E-2-A-1-C-6	1	4	6	5		2	3
	19	F-3-C-4-D-5-E-1-A-2	B-3-F-4-C-6	2	3	6	5		1	4
	20	F-3-C-4-D-5-E-1-A-2	B-4-C-6	2	4	6	5		1	3
	21	F-3-C-6	B-3-F-4-D-5-E-1-A-2	2	3	6	5		1	4
	22	F-3-C-6	B-3-F-4-D-5-E-2	1	3	6	5		2	4
	23	F-3-C-6	B-4-D-5-E-1-A-2	2	4	6	5		1	3
	24	F-3-C-6	B-4-D-5-E-2	1	4	6	5		2	3
	25	F-4-D-5-E-2	B-3-C-6	1	3	6	5		2	4
	26	F-4-D-5-E-2	B-4-F-3-C-6	1	4	6	5		2	3
	27	F-4-D-5-E-1-A-2	B-3-C-6	2	3	6	5		1	4
28	F-4-D-5-E-1-A-2	B-4-F-3-C-6	2	4	6	5	1	3		
<p>Notes</p> <p>(a) B1 cao preferably just 4 lines, but accept if unambiguous.</p> <p>(b) M1 attempt at a path from B or F to 2 or 6 A1 correct path –including change status M1 attempt at a second path from F or B to 6 or 2 A1 correct path –including change status (do not penalise change status twice) A1 correct matching; must follow from 2 correct paths</p>										

Question Number	Scheme	Marks
Q2(a)	(i) All pairs of vertices connected by a path , but not describing complete graph. (ii) No cycles (iii) All nodes connected (accept definition of minimum spanning tree)	B1 B1 B1 (3)
Q2(b)	Kruskal's (algorithm)	B1 (1)
Q2(c)(i)	L-O 56 L-C 60 C-N 62 O-S 63 S-P 43 C-Y 156 Total length 440 (miles)	Using Prim. first 2 correct M1 Next 2 A1 Finish A1 Total A1 =B1
Q2(c)(ii)	Tree correct	 B1 (5) [9]

Q2(c)

Accept weights as indicating arcs.

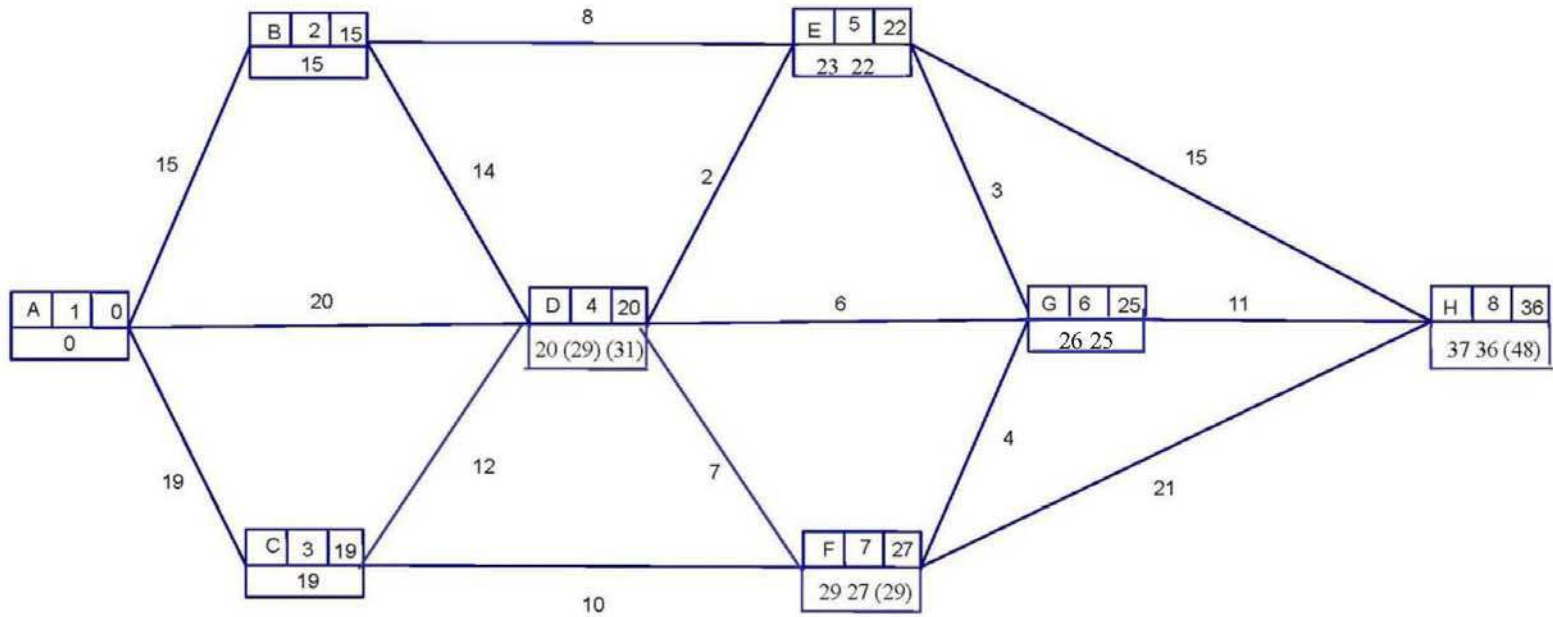
Misreads – award M1 A0 A0 for these:

- Vertices, not edges given L O C N S P Y
- Numbers across top, edges either incorrect or not given: 3 1 4 2 6 5 7.

Also accept these, misreading And not starting at L – again M1A0A0

Started at	Minimum arcs	nodes	Numbers
C	CL,LO,CN,.....	CLONSPY	1243657
N	NC,CL,LO,OS,SP,CY	NCLOSPY	2314657
O	OL,LC,CN,OS,....	OLCNSPY	3241657
P	PS,SO,OL,LC,CN.CY	PSOLCNY	5463127
S	SP.SO,...	SPOLCNY	5463217
Y	YC,CL,LO,CN,..	YCLONSP	2354761

Q3(a)



Clear method to include at least 1 update
 (look at E, F, G or H) MI
 BCDE correct AI
 FGH correct AIft
 Route ADEGH AI
 Total time 36 Minutes AIft (5)

Question Number	Scheme	Marks
Q3(b)	<p>Odd nodes are A, B, C, H</p> <p>$AB + CH = 15 + 25 = 40$</p> <p>$AC + BH = 19 + 22 = 41$</p> <p>$AH + BC = 36 + 22 = 58$</p> <p>(40 is the shortest, repeating AB and CF + FG + GH)</p> <p>Must be choosing from at least two pairings for this last mark</p> <p>Shortest time = $167 + 40 = 207$ minutes. $167 +$ their shortest</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>A1</p> <p>A1ft</p> <p>(5)</p> <p>[10]</p>

Alternate solutions for Question 4

Choosing middle left

0.6	4.0	2.5	3.2	<u>0.5</u>	2.6	0.4	0.3	4.0	1.0	(pivot 0.5)
0.6	4.0	2.5	<u>3.2</u>	2.6	4.0	1.0	0.5	<u>0.4</u>	0.3	(pivots 3.2, 0.4)
<u>4.0</u>	4.0	3.2	0.6	<u>2.5</u>	2.6	1.0	0.5	0.4	<u>0.3</u>	(pivots 4.0, 2.5)
4.0	<u>4.0</u>	3.2	<u>2.6</u>	2.5	<u>0.6</u>	1.0	0.5	0.4	0.3	(pivots 0.6)
4.0	4.0	3.2	2.6	2.5	<u>1.0</u>	0.6	0.5	0.4	0.3	
4.0	4.0	3.2	2.6	2.5	1.0	0.6	0.5	0.4	0.3	

Choosing first

<u>0.6</u>	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	(pivot 0.6)
<u>4.0</u>	2.5	3.2	2.6	4.0	1.0	0.6	<u>0.5</u>	0.4	0.3	(pivots 4.0, 0.5)
4.0	<u>2.5</u>	3.2	2.6	4.0	1.0	0.6	0.5	<u>0.4</u>	0.3	(pivots 2.5, 0.4)
4.0	<u>3.2</u>	2.6	4.0	2.5	<u>1.0</u>	0.6	0.5	0.4	<u>0.3</u>	(pivots 3.2)
4.0	<u>4.0</u>	3.2	<u>2.6</u>	2.5	1.0	0.6	0.5	0.4	0.3	
4.0	4.0	3.2	2.6	2.5	1.0	0.6	0.5	0.4	0.3	

OR (alternate choosing first)

<u>0.6</u>	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	(pivot 0.6)
<u>4.0</u>	2.5	3.2	2.6	4.0	1.0	0.6	<u>0.5</u>	0.4	0.3	(pivots 4.0, 0.5)
<u>4.0</u>	4.0	<u>2.5</u>	3.2	2.6	1.0	0.6	0.5	<u>0.4</u>	0.3	(pivots 2.5, 0.4)
4.0	4.0	<u>3.2</u>	2.6	2.5	<u>1.0</u>	0.6	0.5	0.4	<u>0.3</u>	(pivots 3.2)
4.0	4.0	3.2	<u>2.6</u>	2.5	1.0	0.6	0.5	0.4	0.3	
4.0	4.0	3.2	2.6	2.5	1.0	0.6	0.5	0.4	0.3	

Question 4 sorting into ASCENDING order (full marks if then reversed, otherwise MISREAD)

Middle left

0.6	4.0	2.5	3.2	<u>0.5</u>	2.6	0.4	0.3	4.0	1.0	(pivot 0.5)
<u>0.4</u>	0.3	0.5	0.6	4.0	2.5	<u>3.2</u>	2.6	4.0	1.0	(pivot 0.4, 3.2)
<u>0.3</u>	0.4	0.5	0.6	<u>2.5</u>	2.6	1.0	3.2	<u>4.0</u>	4.0	(pivot 2.5, 4.0)
0.3	0.4	0.5	<u>0.6</u>	1.0	2.5	<u>2.6</u>	3.2	4.0	4.0	(pivot 0.6)
0.3	0.4	0.5	0.6	1.0	2.5	2.6	3.2	4.0	4.0	

Middle right

0.6	4.0	2.5	3.2	0.5	<u>2.6</u>	0.4	0.3	4.0	1.0	(pivot 2.6)
0.6	2.5	0.5	<u>0.4</u>	0.3	1.0	2.6	4.0	<u>3.2</u>	4.0	(pivot 0.4, 3.2)
0.3	0.4	0.6	2.5	<u>0.5</u>	1.0	2.6	3.2	<u>4.0</u>	<u>4.0</u>	(pivot 0.5, 4.0)
0.3	0.4	0.5	0.6	<u>2.5</u>	1.0	2.6	3.2	4.0	4.0	(pivot 2.5)
0.3	0.4	0.5	0.6	<u>1.0</u>	2.5	2.6	3.2	4.0	4.0	(pivot 1.0)

First (1)

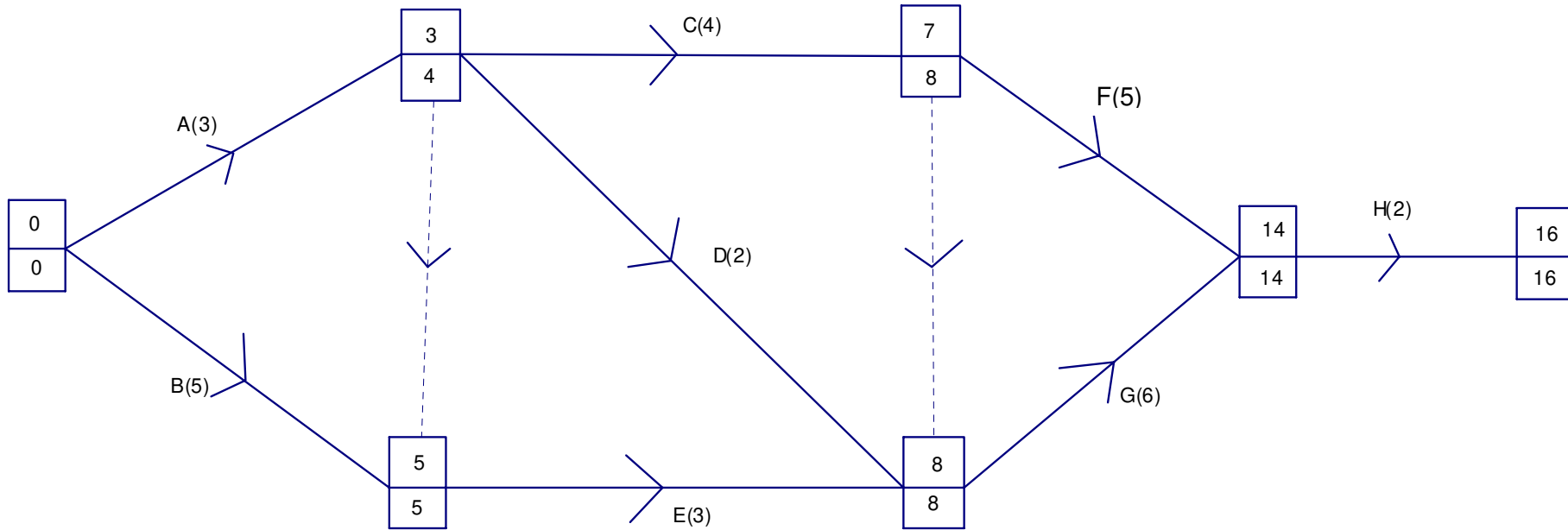
<u>0.6</u>	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	(pivot 0.6)
<u>0.5</u>	0.4	0.3	0.6	<u>4.0</u>	2.5	3.2	2.6	4.0	1.0	(pivot 0.5, 4.0)
<u>0.4</u>	0.3	0.5	0.6	<u>2.5</u>	3.2	2.6	1.0	4.0	4.0	(pivots 0.4, 2.5)
0.3	0.4	0.5	0.6	1.0	2.5	<u>3.2</u>	2.6	4.0	4.0	(pivots 3.2)
0.3	0.4	0.5	0.6	1.0	2.5	2.6	3.2	4.0	4.0	

First (2)

<u>0.6</u>	4.0	2.5	3.2	0.5	2.6	0.4	0.3	4.0	1.0	(pivot 0.6)
<u>0.5</u>	0.4	0.3	0.6	<u>4.0</u>	2.5	3.2	2.6	4.0	1.0	(pivot 0.5, 4.0)
<u>0.4</u>	0.3	0.5	0.6	<u>2.5</u>	3.2	2.6	1.0	4.0	4.0	(pivots 0.4, 2.5)
0.3	0.4	0.5	0.6	1.0	2.5	<u>3.2</u>	2.6	4.0	4.0	(pivots 3.2)
0.3	0.4	0.5	0.6	1.0	2.5	2.6	3.2	4.0	4.0	

Question Number	Scheme						Marks	
Q5								
(a)	S	T	R	R>0?	Output			
	25000	0	17000	y		Line 1		
		3400				Line 2		
			7000			Line 3		
				y		Line 4		
		4450				Line 5		
			-5000			Line 6		
				n		Line 7		
					4450			
						Lines 1 & 2:	M1A1	
						Lines 3-7:	M1A1	
						Output correct:	A1	
							(5)	
(b)	Tax on £25 000 is £4450						B1ft	(1)
(c)	Tax free sum = £8000:						B1	(1)
							[7]	

Q6(c)



Early times
Late times

M1A1
M1A1 (4)

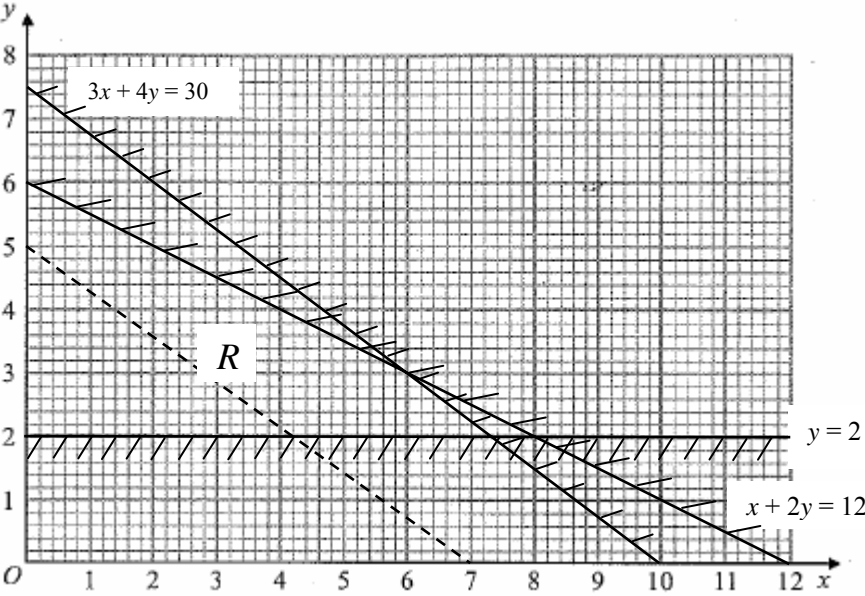
Q6(d) Critical activities: B, E, G, H

B1

Critical path: 16 days

B1ft (2)

Question Number	Scheme	Marks						
Q6(e)	<div style="text-align: center;"> </div> <p style="text-align: center;">At least 6 activities placed including at least 3 floats</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td style="padding-right: 20px;">Critical Activities</td> <td>M1</td> </tr> <tr> <td style="padding-right: 40px;">A + C</td> <td>A1</td> </tr> <tr> <td style="padding-right: 40px;">D + F</td> <td>A1</td> </tr> </table>	Critical Activities	M1	A + C	A1	D + F	A1	<p style="text-align: center;">(4)</p> <p style="text-align: center;">[15]</p>
Critical Activities	M1							
A + C	A1							
D + F	A1							

Question Number	Scheme	Marks
Q7(a)	$x + 2y \leq 12$ ($150x + 300y \leq 1800$)	M1A1 (2)
Q7(b)	$0.9x + 1.2y \leq 9$ $\rightarrow 3x + 4y \leq 30$ (*)	M1 A1 cso (2)
Q7(c)	(You need to buy) at least 2 large cupboards.	B1 (1)
Q7(d)	Capacity C and $140\%C$ So total is $Cx + \frac{140}{100}Cy$ Simplify to $7y + 5x$ (*)	M1 A1cso (2)
Q7(e)	 <p data-bbox="220 1361 686 1545">Graph: $y \geq 2$ $0.9x + 1.2y \leq 12$ ($3x + 4y \leq 30$) $x + 2y \leq 12$ ($150x + 300y \leq 1800$) Lines labelled & drawn with a ruler</p> <p data-bbox="220 1579 574 1624">Shading, Region identified</p>	B1 B1 B1 B1 B1, B1 (6)
Q7(f)	Consider points and value of $5x + 7y$: Or draw a clear profit line (7,2) \rightarrow 49 or $(7 \frac{1}{3}, 2) \rightarrow 50 \frac{2}{3}$, or $(7.3, 2) \rightarrow 50.5$ (6,3) \rightarrow 51 (0,6) \rightarrow 42 (0,2) \rightarrow 14 Best option is to buy 6 standard cupboards and 3 large cupboards.	M1A1 A1 A1 (4)

[17]

Question 7 notes

- (a) 1M1 – correct terms, accept = here, accept swapped coefficients.
1A1 – cao does not need to be simplified.
- (b) 1M1 – correct terms, must deal with cm/m correctly, accept = here.
1A1 – cso **answer given**.
- (c) 1B1 – cao ‘at least’ and ‘2’ and ‘large’.
- (d) 1M1 – ‘1.4’ or ‘5 x 40%’ maybe ‘5+2’ seen, they **must** be **seen** to engage with 140% in some way.
1A1 – cso **answer given**.

Lines should be within 1 small square of correct point at axes.

- (e) 1B1 – correctly drawing $y = 2$.
2B1 – correctly drawing $3x + 4y = 30$ [$0.9x + 1.2y = 12$]
3B1 – correctly drawing $x + 2y = 12$ [$150x + 300y = 1800$], **ft only** if swapped coefficients in (a) (6,0) (2,8).

These next 3 marks are only available for candidates who have drawn at least 2 lines, including at least one ‘diagonal’ line with negative gradient.

- 4B1 – Ruler used. At least 2 lines labelled including one ‘diagonal’ line.
5B1 – Shading, or R correct, b.o.d. on their lines.
6B1 – all lines and R correct.
- (f) 1M1 At least 2 points tested **or** objective line drawn with correct m or 1/m, minimum intercepts 3.5 and 2.5.
1A1 – 2 points correctly tested **or** objective line correct.
2A1 – 3 points correctly tested **or** objective line correct and distinct/labelled.
3A1 – 6 standard and 3 large, accept (6,3) if very clearly selected in some way.

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